

# On Classical dS Vacua in String Theory

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0912.3287 [hep-th]

0812.3886 [hep-th]

0812.3551 [hep-th]

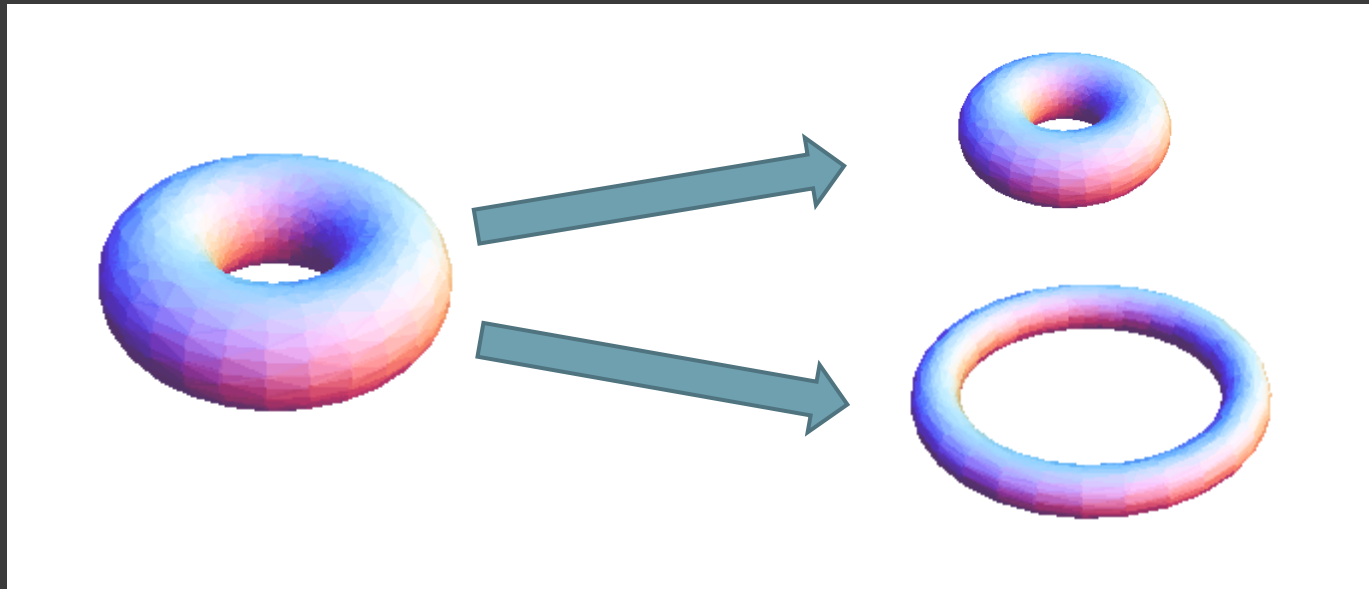
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# Outline

- Motivation
- Type II flux compactifications
- Search for dS vacua and slow-roll inflation in concrete type II models
- Conclusion and Outlook

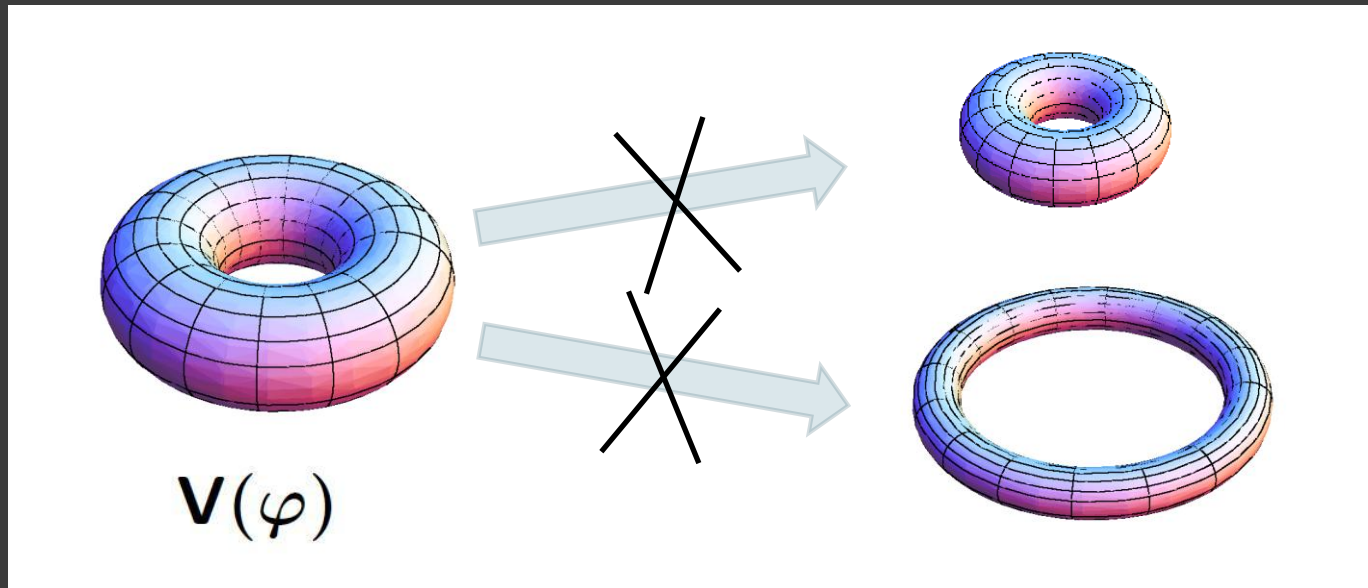
# Motivation

- Supersymmetric compactifications of supergravity/string theory generically lead to massless scalar fields  $\Rightarrow$  moduli problem



# Motivation

- (NSNS and RR) Fluxes, orientifold planes and/or (non-) perturbative corrections stabilize string moduli



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- (NSNS and RR) Fluxes, orientifold planes and/or (non-) perturbative corrections stabilize string moduli
- Interesting for cosmology:

Does  $V(\varphi)$  allow for dS vacua and/or inflation?

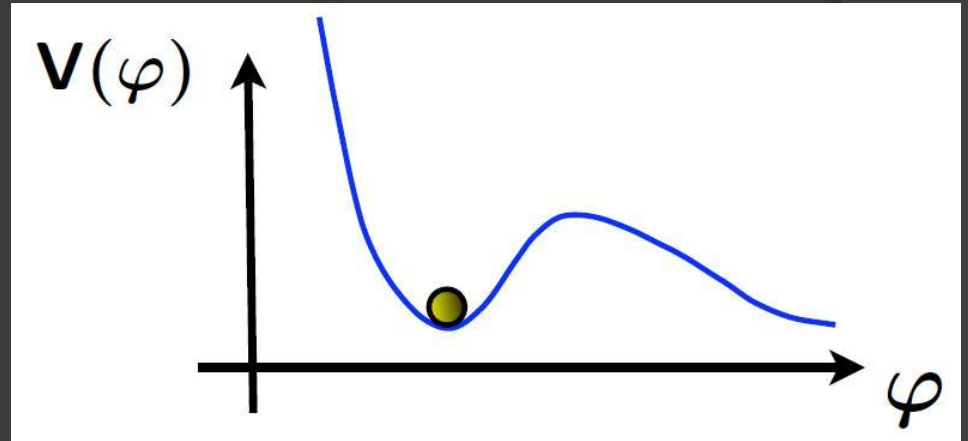
What are the minimal necessary ingredients?

# Motivation

dS vacuum requires

$$\varepsilon \sim (V'/V)^2 = 0$$

$$\eta \sim V''/V > 0$$

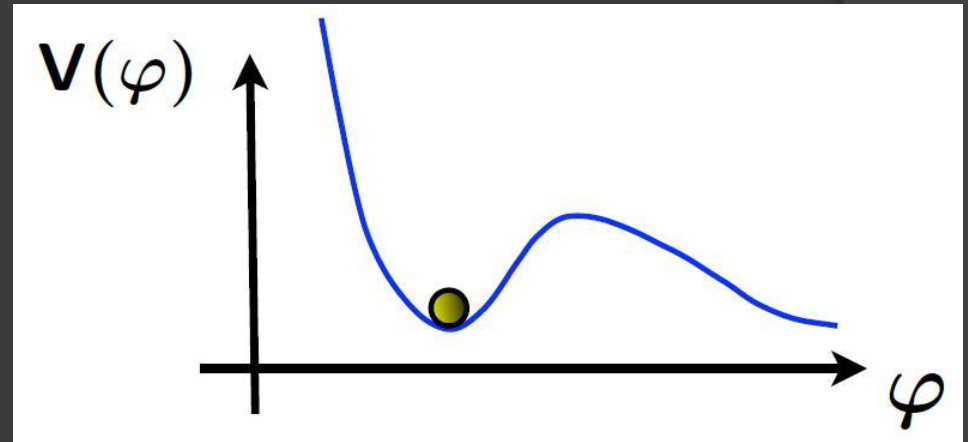


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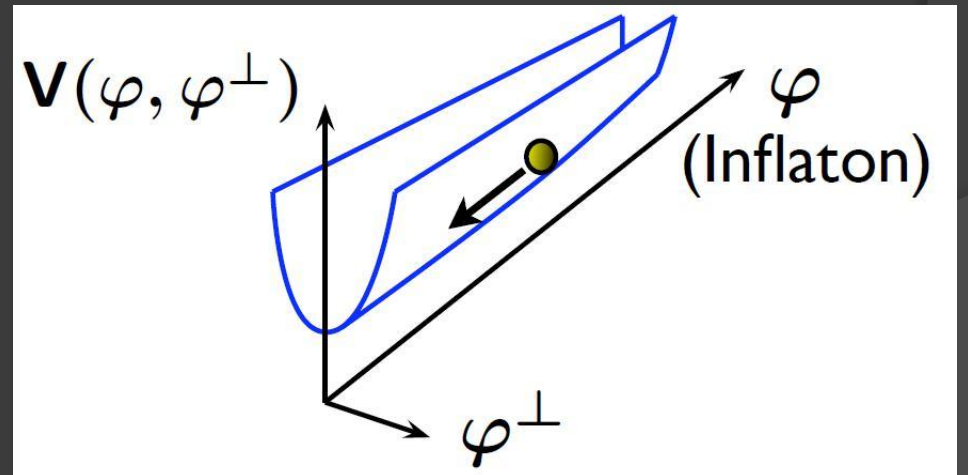
$$\eta \sim V''/V > 0$$



Inflation requires

$$\varepsilon \sim (V'/V)^2 \ll 1$$

$$|\eta| \sim |V''/V| \ll 1$$



# Motivation

Can we find explicit compactifications that lead to fully stabilized dS vacua at tree-level?



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Need negative tension objects (O-planes)

Gibbons  
deWit, Smit, Hari Dass  
Maldacena, Nuñez

⇒ Type IIA/IIB string theory

# Type II Flux Compactifications

Can we find explicit compactifications that lead to fully stabilized dS vacua at tree-level?

$$\rho = (\text{vol}_6)^{1/3}, \quad \tau = e^{-\phi} \sqrt{\text{vol}_6}$$

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$$V_H \propto \tau^{-2} \rho^{-3}, \quad V_{F_p} \propto \tau^{-4} \rho^{3-p}, \quad V_{O_q} \propto \tau^{-3} \rho^{\frac{q-6}{2}}, \quad V_{R_6} \propto \tau^{-2} \rho^{-1}$$

$$\text{IIA: } p \in \{0, 2, 4, 6\}, q \in \{4, 6, 8\}, \quad \text{IIB: } p \in \{1, 3, 5\}, q \in \{3, 5, 7, 9\}$$

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$$V = V_H + \sum_p V_{F_p} + \sum_q V_{Oq} + V_{R_6}, \quad V_H, V_{F_p} \geq 0, \quad V_{Oq} \leq 0$$

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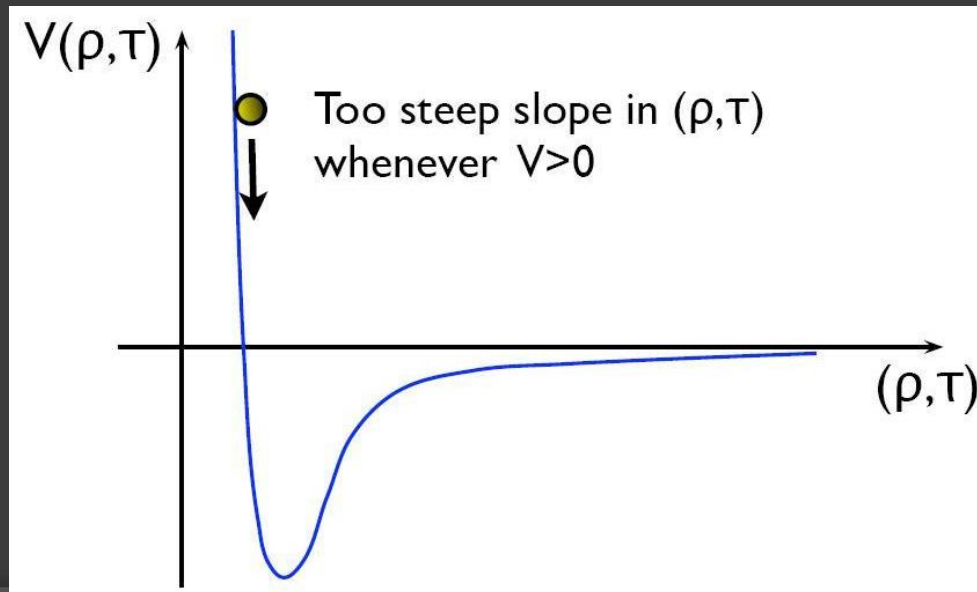
**no slow-roll:**  $\varepsilon = \frac{K^{\bar{i}\bar{j}}\partial_{\bar{i}}V\partial_{\bar{j}}V}{V^2} \geq \frac{c^2}{4a^2 + 3b^2} \approx O(1)$

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Can find  $a, b$  such that  $(-a\tau\partial_\tau - b\rho\partial_\rho)V \geq cV$ ,  $c > 0$ ,

- whenever  $p + q - 6 \geq 0$ ,  $\forall p, q$ , for  $V_{R_6} \propto -R_6 \leq 0$ .
- whenever  $p + q - 8 \geq 0$ ,  $\forall p, q$ ,<sup>1)</sup> for  $V_{R_6} \propto -R_6 > 0$ .

1) O3-planes with  $F_5$ -flux is also possible.

# Type II Flux Compactifications

Can we find explicit compactifications that lead to fully stabilized classical dS vacua?

Curvature	No-go if	No no-go IIA	No no-go IIB
$V_{R_6} \propto -R_6 \leq 0$	$p + q - 6 \geq 0, \forall p, q$	$F_{0,H}, O4\text{-planes}$	$F_{1,H}, O3\text{-planes}$
$V_{R_6} \propto -R_6 > 0$	$p + q - 8 \geq 0, \forall p, q$	$F_0, O4\text{-planes}$	$F_1, O3\text{-planes}$
		$F_2, O4\text{-planes}$	$F_3, O3\text{-planes}$
		$F_0, O6\text{-planes}$	$F_5, O3\text{-planes}$
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Minimal ingredients needed to evade no-go theorem in the  $(\rho, \tau)$ -plane.

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Need low dimensional  $Oq$ -planes with low rank RR-fluxes.

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Spaces with negative integrated curvature favored.

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CY<sub>3</sub> has  $R_6=0$ : IIA with  $F_0, F_2, F_4, F_6, H, O6$

IIB with  $F_3, H, O3$

Hertzberg, Kachru, Taylor, Tegmark 0711.2512 [hep-th]

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$R_6=0$ : Need 1-cycles/1-forms for O4-planes/F1-flux.

What about  $T^6$  or  $T^2 \times K3$ ?

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$F_0$  flux needs to be odd under O4 orientifold projection.

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$F_{1/5}$  flux needs to be even under  $O3$  orientifold projection.



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Curvature and O3 orientifold projection:

$$de^i = -\frac{1}{2} f_{jk}^i e^j \wedge e^k, \quad \sigma_{O3} : e^i \rightarrow -e^i \quad \Rightarrow \quad f_{jk}^i = 0$$

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Probably always one Kähler modulus unstabilized which leads to a runaway direction.

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Full moduli stabilization in principle possible!

# Type II Flux Compactifications

Can we find explicit compactifications that lead to fully stabilized classical dS vacua?

Assumptions:

- Restrict to bulk moduli and neglect blow-up sector
- Restrict to the closed string sector (no D-branes)
- Take O-planes to be smeared over transverse directions
- Consider only compactifications that give a 4d

$$\mathcal{N} = 1 \text{ action}$$

# Type II Flux Compactifications

Flux compactifications that give a 4d  $\mathcal{N} = 1$  action

- $CY_3$  with O6, O3/O7 or O5/O9

Grimm, Louis hep-th/0403067, hep-th/0412277

DeWolfe, Giryavets, Kachru, Taylor hep-th/0505160

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- **SU(3)-structure** with **O6**, O3/O7 or O5/O9

Silverstein 0712.1196 [hep-th]

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Danielsson, Haque, Shiu, Van Riet 0907.2041 [hep-th]

de Carlos, Guarino, Moreno 0907.5580, 0911.2876 [hep-th]

Danielsson, Koerber, Van Riet 1003.3590 [hep-th]

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Danielsson, Koerber, Van Riet 1003.3590 [hep-th]

- **SU(2)-structure** with **O5/O7** or **O4/O6/O8**

C. Caviezel, TW, M. Zagermann 0912.3287 [hep-th]

# SU(n)-structure manifolds, $n=2,3$

Calabi-Yau is special case of SU(n)-structure manifold

$$\nabla \zeta = 0 \Rightarrow R_{mn} = 0 \Rightarrow V_{R_6} = 0 \Rightarrow \text{No-go theorem}$$



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Problem: What are the relevant light fields?

$$\text{CY}_3: \quad J_{mn} = i\zeta_+^\dagger \gamma_{mn} \zeta_+ \quad \Omega_{mnp} = \zeta_-^\dagger \gamma_{mnp} \zeta_+$$

$$\nabla \zeta = 0 \Rightarrow dJ, d\Omega = 0 \Rightarrow \text{Expand in harmonic forms}$$

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Expansion basis, moduli?

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- Generic case not understood

Kashani-Poor, Minasian hep-th/0611106

Graña, Louis, Waldram hep-th/0612237

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- Examples of SU(n)-structure manifolds include twisted tori and coset spaces  $G/H$

Dabholkar, Hull, Reid-Edwards

Cvetic, Liu, Schulz

Robbins, Ihl, TW

Graña, Minasian, Petrini, Tomasiello

Caviezel, Koerber, Körs, Lüst, Tsimpis, Zagermann

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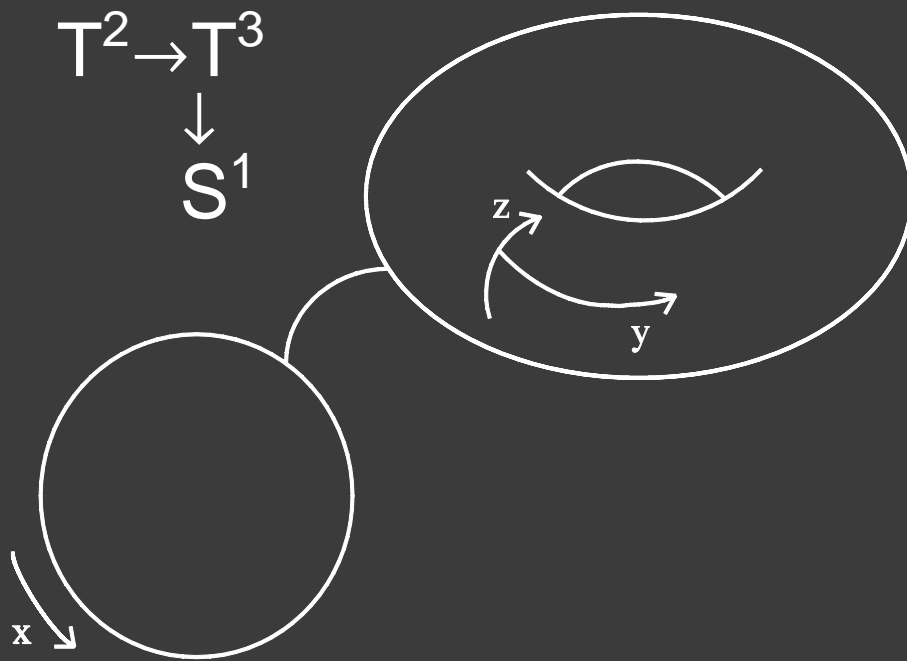
Graña, Minasian, Petrini, Tomasiello

Caviezel, Koerber, Körs, Lüst, Tsimpis, Zagermann

- Natural expansion basis exists:  $G$  invariant forms
- Models expected to be consistent truncations ( $\Rightarrow$  potential instability in other sector)

Cassani, Kashani-Poor 0901.4251 [hep-th]

# Generalized NSNS-flux: H-flux



$$ds^2 = dx^2 + dy^2 + dz^2$$

$$x, y, z \sim x, y, z + 1$$

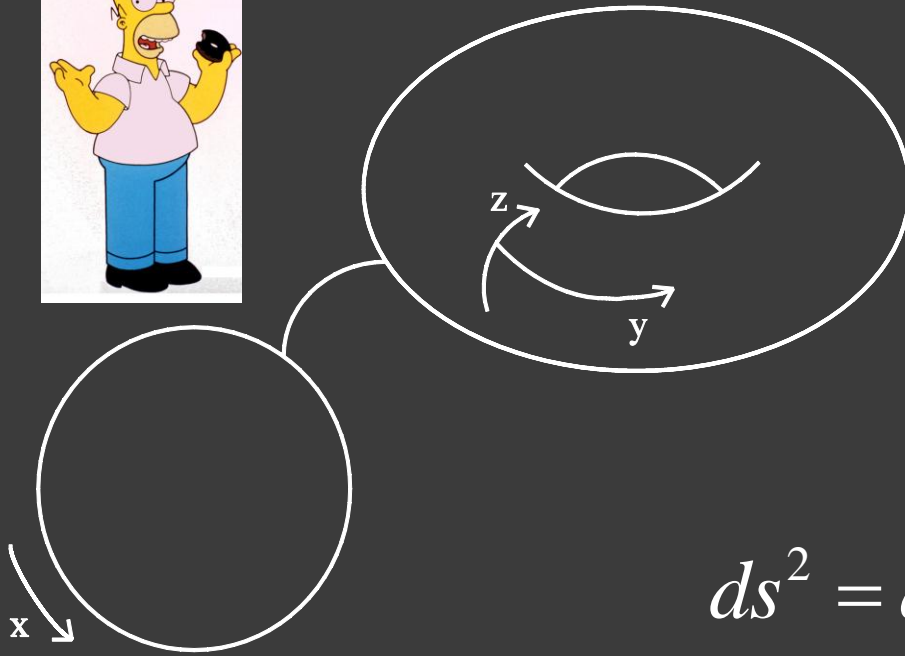
$$H = N dx \wedge dy \wedge dz$$

$$\int_{T^3} H = N$$

$$B = Nx dy \wedge dz$$

If we go around the base  $x \rightarrow x + 1$ , the B-field on the fiber gets shifted  $B_{yz} \rightarrow B_{yz} + N$ .

# Generalized NSNS-flux: (geo) metric flux



T-duality along  $z$ :

$$B = 0 \Rightarrow H = 0$$

$$ds^2 = dx^2 + dy^2 + (dz + Nx dy)^2$$

If we go around the base  $x \rightarrow x + 1$ , the fiber gets twisted  $y \rightarrow y, z \rightarrow z - Ny$ .



# Generalized NSNS-flux: (geo) metric flux

- The new space is not a torus anymore. It is often called twisted torus.
- It has the global 1-forms

$$e^x = dx, \quad e^y = dy, \quad e^z = dz + Nxdy.$$

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- It has the global 1-forms

$$e^x = dx, \quad e^y = dy, \quad e^z = dz + Nx dy.$$

- The  $H_{ijk}$ -flux got turned into “metric flux”  $f_{jk}^i$

defined by  $de^i = -\frac{1}{2} f_{jk}^i e^j \wedge e^k$ .

- We expand our fields and fluxes in terms of the  $e^i$  so that they won't be closed anymore.

# Generalized NSNS-flux: (geo) metric flux

- The new space is not a torus anymore. It is often called twisted torus.

- It has the global 1-forms

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- The twisted torus is not Ricci flat but has  $R_3 = -\frac{N^2}{2}$ .

# Type IIA on SU(3)-structure

SU(3)-structure space with **negative curvature** and  
**O6**-planes,  $F_{0,2,4,6}$ , H-flux evade no-go theorem in the  
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**but concrete models have many more directions:**

$$V = V(\tau, \rho, \varphi^\perp)$$

Are there refined no-go theorems involving the  $\varphi^\perp$ ?

# Type IIA on SU(3)-structure

New no-go theorems using other directions in moduli space?

For example models with factorization of Kähler sector:

$$vol_6 = \kappa_{abc} k^a k^b k^c = k^0 \tilde{\kappa}_{de} k^d k^e = vol_2 \cdot vol_4, \quad d, e \neq 0$$

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Idea:

$$V(\tau, \rho, \dots) \rightarrow V(\tau, k^0, k^d, \dots)$$

Are there refined no-go theorems using the  $\tau, k^0, k^d$ - directions? Under what assumptions?

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and restrictions on curvature (“metric fluxes”), e.g.

$$J = k^0 w_0 + k^d w_d$$

$$dw_0 = 0, dw_d \neq 0: -\tau \partial_\tau V - k^0 \partial_{k^0} V \geq 3V \Rightarrow \varepsilon \geq \frac{9}{5},$$

$$dw_0 \neq 0, dw_d = 0: -2\tau \partial_\tau V - k^d \partial_{k^d} V \geq 6V \Rightarrow \varepsilon \geq 2.$$

Flauger, Robbins, Paban, TW 0812.3886 [hep-th]

Caviezel, Koerber, Körs, Lüst, TW, Zagermann 0812.3551 [hep-th]

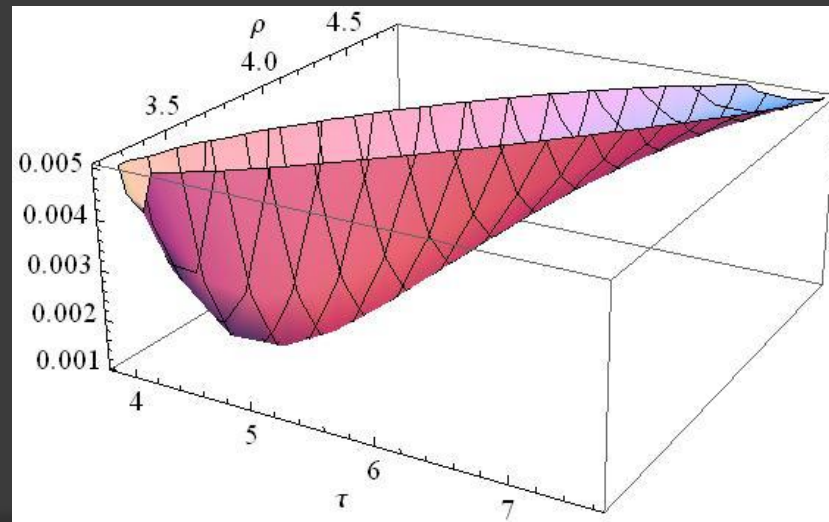
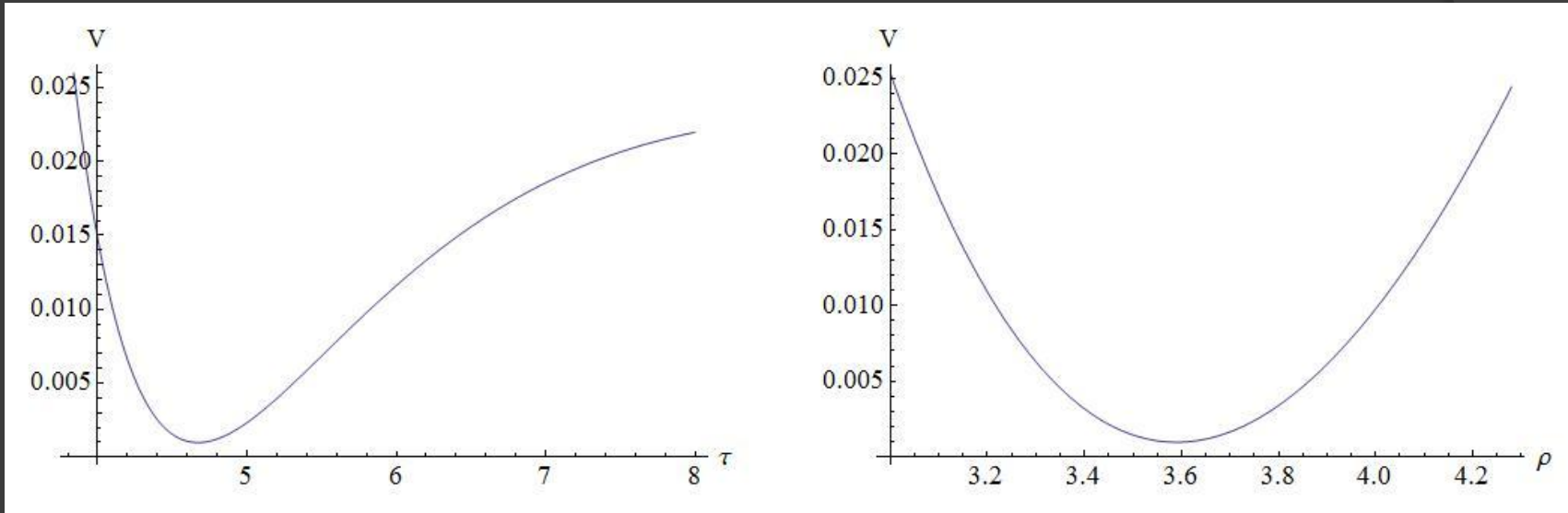


# Type IIA on SU(3)-structure

New no-go theorems using other directions in moduli space:

- Exclude almost all models (6 cosets, 10 twisted tori) that were studied
- $\check{T}^6/Z_2 \times Z_2$  and  $S^3 \times S^3/Z_2 \times Z_2$  evade all known no-go theorems. Numerically we indeed find  $\varepsilon \approx 0$ !

# Type IIA on $S^3 \times S^3$

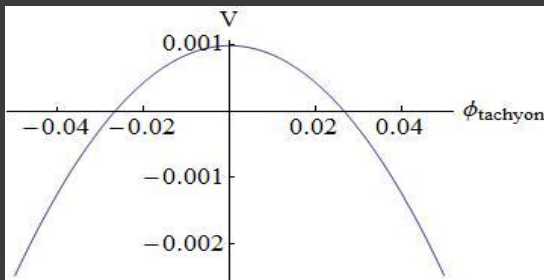


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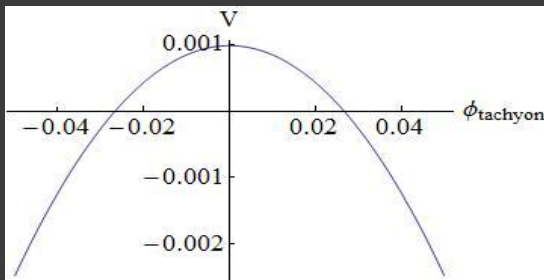


Flauger, Robbins, Paban, TW 0812.3886 [hep-th]  
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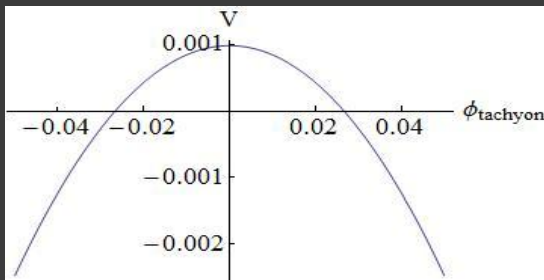
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Covi, Gomez-Reino, Gross, Louis, Palma, Scrucca 0804.1073 [hep-th]  
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- dS extremum for  $S^3 \times S^3/Z_2 \times Z_2$  lifts to 10d

Covi, Gomez-Reino, Gross, Louis, Palma, Scrucca 0804.1073 [hep-th]  
Covi, Gomez-Reino, Gross, Louis, Palma, Scrucca 0805.3290 [hep-th]

Danielsson, Koerber, Van Riet 1003.3590 [hep-th]

# Type IIB on SU(2)-structure

- SU(2)-structure compactifications with O5/O7 orientifold projections  $\Rightarrow N = 1$  in 4d
- SU(2)-structure manifolds have 1- and 5-forms  $\Rightarrow$  RR fluxes  $F_1, F_3, F_5$  for IIB

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- **Can stabilize all moduli at tree-level in a supersymmetric AdS vacuum with large volume and small string coupling**

Caviezel, TW, Zagermann 0912.3287 [hep-th]



# Type IIB on SU(2)-structure

Type IIB on  $T^2 \times T^4 / Z_2$  with  
O5-planes and O7-planes  
SU(2)-structure

O-plane	$T^2$		$T^4 / Z_2$			
	1	2	3	4	5	6
O5			X	X		
O5					X	X
O7	X	X	X		X	
O7	X	X		X		X

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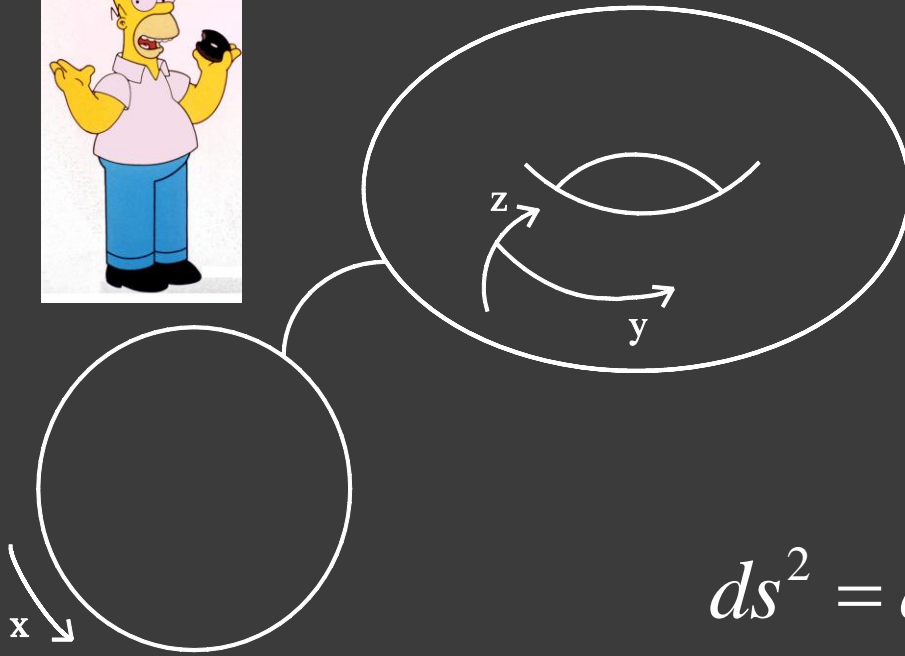
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O7	X	X		X		X

↑ T-duality

Type IIA on  $T^6/Z_2 \times Z_2$  with  
O6-planes  
SU(3)-structure

O-plane	1	2	3	4	5	6
O6	X		X	X		
O6	X				X	X
O6		X	X		X	
O6		X		X		X

# Generalized NSNS-flux: (geo) metric flux



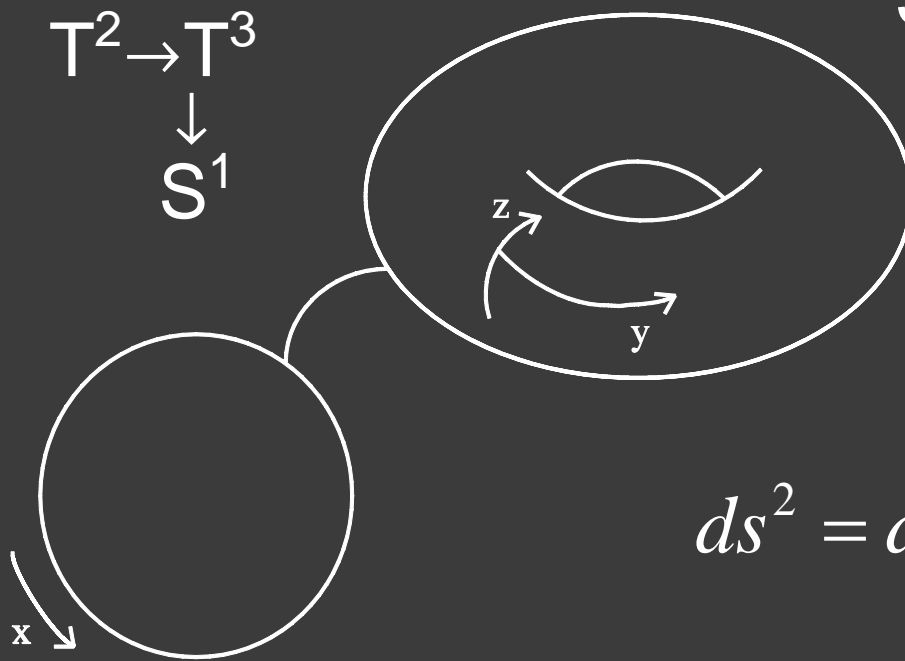
T-duality along z:

$$B = 0 \Rightarrow H = 0$$

$$ds^2 = dx^2 + dy^2 + (dz + Nx dy)^2$$

If we go around the base  $x \rightarrow x + 1$ , the fiber gets twisted  $y \rightarrow y, z \rightarrow z - Ny$ .

# Generalized NSNS-flux: non-geometric flux



Second T-duality along  $y$ :

$$B_{yz} = \frac{Nx}{1 + N^2 x^2}$$

$$ds^2 = dx^2 + \frac{1}{1 + N^2 x^2} (dy^2 + dz^2)$$

If we go around the base  $x \rightarrow x + 1$ ,  $g$  and  $B$  are not periodic in any obvious sense. The space is only locally geometric but not globally.

# Type IIB on $SU(2)$ -structure

T-dual to  $SU(3)$ -structure but might lead to new examples:

- $SU(3)$ - and  $SU(2)$ -structure spaces have metric-flux
- T-duality might lead to non-geometric spaces  
⇒ supergravity applicable in T-dual description?

Wecht 0708.3984 [hep-th]

- $SU(2)$ -structure compactifications not T-dual to geometric  $SU(3)$ -spaces are new

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# Type IIB on SU(2)-structure

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- Natural split of Kähler and complex structure moduli:  
$$vol_6 = vol_2 \cdot vol_4, \quad \text{Im}(\Omega_2), \quad dvol_2 \wedge \text{Re}(\Omega_2)$$
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- Can derive no-go theorems to exclude dS vacua and slow-roll in several concrete examples
- $S^3 \times S^3$  example again evades all no-go theorems.

Numerically we indeed find  $\varepsilon \approx 0$  but  $\eta \approx -3$ .

Caviezel, TW, Zagermann 0912.3287 [hep-th]



# Conclusions

- General no-go theorems against tree-level dS vacua and slow-roll inflation exists
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- Negative curvature spaces more promising
- Type IIA on  $SU(3)$ -structure with O6-planes and type IIB on  $SU(2)$ -structure with O5/O7-planes allow for stabilization of all closed string moduli
- Many no-go theorems for explicit examples
- Can find explicit numerical dS extrema but only with one tachyonic direction

# Outlook / Future research

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Villadoro, Zwirner hep-th/0602120

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# THANK YOU!